# UNIVERSITY OF TORONTO SCARBOROUGH Department of Computer and Mathematical Sciences <br> <br> STAB22H3 Statistics I <br> <br> STAB22H3 Statistics I <br> Duration: 1 hour and 45 minutes 

Last Name: $\qquad$ First Name: $\qquad$
Student number: $\qquad$
Aids allowed:

- One handwritten letter-sized sheet (both sides) of notes prepared by you
- Non-programmable, non-communicating calculator

Standard normal distribution tables are attached at the end.
This test is based on multiple-choice questions. All questions carry equal weight. On the Scantron answer sheet, ensure that you enter your last name, first name (as much of it as fits), and student number (in "Identification").

Mark in each case the best answer out of the alternatives given (which means the numerically closest answer if the answer is a number and the answer you obtained is not given.)

Also before you begin, complete the signature sheet, but sign it only when the invigilator collects it. The signature sheet shows that you were present at the exam.

There are 15 pages including this page. Please check to see you have all the pages.

Good luck!!

1. In an effort to improve the overall health and well-being of its employees, a large corporation distributed a written survey to each of its 1400 employees. Data collected included number of hours worked per week, number of hours spent exercising per week, number of hours spent enjoying hobbies per week, and number of hours spent with family/friends per week. Which of the following choices correctly identifies the W's (Note in this question is only interested in three W's: Who, What and Why. Please identify the choice that identifies all these three W's correctly.)
A) Who: The 1400 employees; What: Number of hours spent exercising per week.; Why: To devise a health club plan
B) Who: The 1400 employees; What: Number of hours worked per week, number of hours spent exercising per week, number of hours spent enjoying hobbies per week, and number of hours spent with family/friends per week; Why: To improve the health and well-being of its employees
C) Who: Large corporations; What: Number of hours worked per week.; Why: To improve the health and well-being of its employees
D) Who: The 1400 employees; What: Overall job satisfaction; Why: To improve the health and well-being of its employees
E) Who: A large corporation; What: Overall job satisfaction; Why: To improve the health and well-being of its employees

Solution: Note: This is question 6 Deveaux quiz bank.Chapter 2 page 3.
2. A study of 2007 model automobiles was conducted. In the study the following variables were considered: the Region in which the car was manufactured (Europe, North America, Asia); the Type of automobile (compact, midsize, large), volume of the engine in liters, and the type of Fuel used (regular, premium, $85 \%$ Ethanol). The variables Region, Type, volume, and Fuel are, respectively are:
A) quantitative, categorical, categorical, quantitative.
B) categorical, quantitative, quantitative, categorical.
C) categorical, categorical, quantitative, quantitative.
D) categorical, categorical, quantitative, categorical.
E) Unable to determine without knowing the values of the various variables.
3. Based on data from the National Health Survey, the distribution of weights for adult males in the U.S. has a mean weight of 173 pounds and a standard deviation of 30 pounds. Suppose the distribution of weights was skewed to the left. The median weight is one of the following values. Which of the following values is most likely the value of the median weight?
A) 173 pounds
B) 163 pounds
C) 143 pounds
D) 188 pounds
E) 150 pounds

Solution: For left-skewed distributions, mean $<$ median, i.e. mean $>173$.
4. Data on the mileage per gallon of 20 randomly selected cars are listed below. The values are ordered for convenience.
$12,13,15,16,16,17,18,18,19,19,20,20,22,23,24,26,26,27,27,29$

What is the interquartile range for the mileage data?
A) 8.5 miles per gallon
B) 16.5 miles per gallon
C) 17 miles per gallon
D) 25 miles per gallon
E) 12.75 miles per gallon

Solution: $Q 1=16.5, Q 3=(24+26) / 2=25$ and so $I Q R=Q 3-Q 1=25-16.5=$ 8.5
5. The table below gives the results of a survey of 800 college seniors regarding their undergraduate major and whether or not they plan to go to graduate school.

| Graduate School | Business | Engineering | Others |
| :--- | :---: | :---: | :---: |
| Yes | 70 | 84 | 126 |
| No | 182 | 208 | 130 |

What percentage of the students does not plan to go to graduate school?
A) 280
B) 65
C) 32
D) 35
E) 25

## Solution:

| Graduate School | Business | Engineering | Others | Total |
| :--- | :---: | :---: | :---: | :---: |
| Yes | 70 | 84 | 126 | 280 |
| No | 182 | 208 | 130 | 520 |
| Total | 252 | 292 | 256 | 800 |

Percentage of the students not planning to go to graduate school $=\frac{520}{800}=0.65=65$ percent.
6. Using the data in question 5 above, among those students who are majoring in business, what percentage plans to go to graduate school?
A) 27.78
B) 8.75
C) 72.22
D) 70
E) 25

Solution: There are 252 business students and 70 of them are planning to go to graduate school and so the percentage $=\frac{70}{252} \times 100=27.78$ percent.
7. Using the data in question 5 above, among the students who plan to go to graduate school, what percentage is business majors?
A) 27.78
B) 8.75
C) 72.22
D) 70
E) 25

Solution: There are 280 students who are planning to go to graduate school and 70 of them are business majors and so the percentage $=\frac{70}{280} \times 100=25$ percent.
8. For a simple linear regression model, suppose we fitted a least squares regression line and obtained $\hat{y}=5+3 x$. What is the residual associated with the point $(x, y)=(4,19)$ ?
A) -13

Question 8 continues on the next page...
B) -2
C) 13
D) 17
E) 2

Solution: $\hat{y}=5+3 \times 4=17$ and residual $=y-\hat{y}=19-17=2$.
9. For simple linear regression, the fitted regression line obtained using the method of least squares is
A) the line which makes the sample correlation coefficient as close to +1 or -1 as possible.
B) the line which best splits the data in half, with $50 \%$ of the data points lying above the regression line and $50 \%$ of the data points lying below the fitted regression line.
C) the line which minimizes the number of data points that do not pass through the regression line.
D) the line that minimizes the sum of the squared residuals.
E) the line which guarantees that the error terms will be normally distributed.
10. The time to complete a standardized exam is approximately normal with a mean of 70 minutes and a standard deviation of 10 minutes. Using the 68-95-99.7 rule, if students are given 90 minutes to complete the exam, what percentage of students will not be able finish in this time (i.e. they need more than 90 minutes)?
A) $32 \%$
B) $16 \%$
C) $5 \%$
D) $2.5 \%$
E) $0.0015 \%$

Solution: 90 is 2 standard deviations above the mean and the area beyond two standard deviations $=5 / 2=2.5 \%$.
11. You wish to study which car colors are the most popular among students. Which of the following would be the most useful?
A) Boxplot
B) Histogram
C) Pie chart
D) stemplot
E) Five-number summary

Solution: Car colour is a categorical variable. Pie chart is the only graph available for categorical variables. All other choices above are for quantitative variables.
12. Of the following measures: mean, median, $I Q R$ (inter quartile range), and standard deviation, which measures are resistant to outliers?
A) Mean and median
B) Median and $I Q R$
C) Mean and standard deviation
D) Median and standard deviation
E) None of the above
13. The mean income per household in a certain state is $\$ 9500$ with a standard deviation of $\$ 1750$. The distribution of income is Normal. The middle $95 \%$ of incomes are between what two values?
A) $\$ 5422$ and $\$ 13578$
B) $\$ 6070$ and $\$ 12930$
C) $\$ 6621$ and $\$ 12379$
D) $\$ 7260$ and $\$ 11740$
E) $\$ 8049$ and $\$ 10951$

Solution: $9500-1.96 \times 1750=6070,9500+1.96 \times 1750=12930$. If we use the $68-95-99.7$ rule, $9500-2 \times 1750=6000,9500+2 \times 1750=13000$. The closest is still (B)
14. Heights of males are approximately normally distributed with a mean of 170 cm and a standard deviation of 8 cm . What proportion of males are taller than 176 cm ?
A) 0.7500
B) 0.6000
C) 0.2734
D) 0.2500
E) 0.2266

Solution: $Z=\frac{176-170}{8}=0.75$. Table value for $Z=0.75$ is 0.7734 and so the proportion taller than 176 is $1-0.7734=0.2266$.
15. The annual salaries of employees in a company have a Normal distribution with mean $\$ 48000.16 \%$ of the employees in this company have annual salaries of $\$ 60000$ and above. What is the standard deviation of the annual salaries of employees in this company? Choose the closest answer if the exact answer is not among the choices below. (Hint: 68-95-99.7 rule can be helpful. You can also answer this question without using 68-95-99.7 rule.)
A) $\$ 6000$
B) $\$ 12000$
C) $\$ 15000$
D) $\$ 18000$
E) $\$ 24000$

Solution: Based on the 68-95-99.7 rule, $\sigma=60000-48000=12000$. Normal tables should give a value close to this, though not necessary exactly equal to this.
16. A professor is interested in determining if one could predict the score on a statistics exam from the amount of time spent studying for the exam. What is the explanatory variable in this study?
A) the professor
B) the score on the exam
C) the amount of time spent studying for the exam
D) the number of students who wrote the exam
E) the number of questions in the exam
17. The general manager of a chain of furniture stores believes that experience is the most important factor in determining the level of success of a salesperson. To examine this belief she records last month's sales (in $\$ 1,000 \mathrm{~s}$ ) and the years of experience of 10 randomly selected salespeople. Summary statistics from this study are given below:

Descriptive Statistics: Experience, Sales

| Variable | N | Mean | StDev |
| :--- | ---: | ---: | ---: |
| Experience | 10 | 8.20 | 6.21 |
| Sales | 10 | 17.50 | 6.88 |
|  |  |  |  |
|  |  |  |  |
| Correlation of |  |  |  |

What is the slope of the least squares regression line of Sales on Experience?
A) 0.88
B) 2.08
C) 0.46
D) 1.08
E) 8.20

Solution: $b_{1}=r \frac{s_{y}}{s_{x}}=0.977 \times \frac{6.88}{6.21}=1.082409018$
18. Using information in question 17 above, what proportion of the variability in sales is explained by the linear regression of Sales on Experience? Choose the closest.
A) 0.98
B) 0.39
C) 0.95
D) 0.46
E) 0.76

Solution: This means $R^{2}=0.977^{2}=0.954529$
19. The scatterplot of the data on sale price ( $y$ in millions of dollars) and size ( $x$, thousands of sq. ft) for 10 large industrial properties that appeared in the paper " Using Regression Analysis in Real Estate Appraisal" (Appraisal Journal [2002]), is shown below:


Which of the following numbers is closest to the correlation between $x$ and $y$ ?
A) -1
B) -0.5
C) 0
D) 0.6
E) 1

Solution: The correlation is positive, but perfectly on a straight line and so not +1 . The exact value for this data set was 0.7.
20. For data on a quantitative variable, which of the following is true?
A) If the distribution is symmetric, then the range is an appropriate measure of the center.
B) If the distribution is symmetric, then the standard deviation is an appropriate measure of the center.
C) If the distribution is skewed, then the mean is an appropriate measure of the center.
D) If the distribution is skewed, then the median is an appropriate measure of the center.
E) If the distribution is skewed, then the standard deviation is an appropriate measure of the spread.
21. Last year a small statistical consulting company paid each of its five statistical clerks $\$ 22,000$, two statistical analysts $\$ 50,000$ each, and the senior statistician $\$ 270,000$. How many employees in this company earned less than the mean salary?
A) 0
B) 4
C) 5
D) 6
E) 7

Solution: $(22000 \times 5+50000 \times 2+270000) / 8=60000$
22. The Programme for International Student Assessment (PISA) reported 2006 average mathematics performance scores for 15 year olds in 32 countries. These scores are given below (for convenience they are sorted in increasing order):

| 406 | 424 | 459 | 462 | 466 | 474 | 480 | 484 | 490 | 490 | 491 | 492 | 495 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 495 | 496 | 498 | 501 | 502 | 504 | 505 | 506 | 510 | 513 | 520 | 520 | 522 |
| 523 | 527 | 530 | 531 | 547 | 548 |  |  |  |  |  |  |  |

Question 22 continues on the next page...

Some useful summary statistics (StatCrunch output) of these scores are given below:

Descriptive Statistics: Score

| Variable | $N$ | Mean | StDev | Q1 | Median | Q3 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| Score | 32 | 497.22 | 30.93 | 485.50 | 499.50 | 520.00 |

Based on $1.5 \times I Q R$ rule, how many outliers are there in this data set?
A) There are no outliers.
B) Only one outlier.
C) Only two outliers.
D) Only three outliers.
E) More than three outliers.

Solution: Upper fence $=520+1.5 \times(520-485.5)=571.75$.
Lower fence $=485.5-1.5 \times(520-485.5)=433.75$.
406 and 424 are smaller than the lower fence and so they are outliers.
23. The boxplots below displays a comparison of blood cholesterol measurements for three groups of people (group A, B and C):


Read the following statements based on the above boxplots:
I The third quartile for group $A$ is less than the first quartile for group B.
II More than 25 percent of the people in group C have higher cholesterol levels than the person with the highest level in group A.
III The median for group B is greater than the mean for group B.

The above statements may or may not be true. Based on the information in the boxplots above, which statement is true?
A) Only statement I is true
B) Only statement II is true
C) Only statements I and II are true
D) Only statements II and III are true
E) none is true
24. The times that it takes students to complete a STAB22 midterm test are Normally distributed with a mean of 155 minutes with standard deviation of 10 minutes. How much time should be allowed if we wish to ensure that 9 out of 10 students (on average) can complete it? (round your answer to the nearest minute).
A) 170 or more
B) 169
C) 168
D) 167
E) 166 or less

Solution: $155+1.282 \times 10=167.82$
25. In a simple linear regression problem, the least squares regression line is given by $y=$ $2.15-1.75 x$, and the coefficient of determination is 0.81 . What is the correlation between $x$ and $y$ ?
A) 0.81
B) -0.81
C) 0.9
D) -0.9
E) none of the above options gives the correct correlation between $x$ and $y$

Solution: $r=-\sqrt{0.81}=-0.9$, negative because the slope is negative.
26. The two-way table below shows the distribution of the number of members in a fitness club classified by two variables.

|  | Women | Men |
| :--- | :---: | :---: |
| Vegetarian | 9 | 3 |
| Non-vegetarian | 8 | 10 |

Based on this information, which of the following statements is true?
A) Women in that club are more likely to be vegetarian than men.
B) Women in that club are more likely to be non-vegetarian than men.
C) Women in that club are less likely to be vegetarian than men.
D) Among vegetarians in this club, there are more men than women.
E) None of the above statements is true.

Solution: Compare conditional proportions for men and women:
Proportion of vegetarians among women $=9 /(9+8)=0.5294117647$
Proportion of vegetarians among men $=3 / 13=0.2307692308$.
27. The data set is displayed in the stemplot below:

```
Decimal point is 1 digit(s) to the right of the colon.
0 : 3
1 : 002
2 : 389
3 : 025558
4 : 13
```

Based on information in this stemplot, which of the following statements is FALSE? (Note: only one statement is false.)
A) The median is 30 .
B) The range is 40 .
C) There are no outliers.
D) The third quartile is 35 .
E) The mean is greater than 30 .

Solution: The distribution is left-skewed and so the mean is less than the median. i.e. the mean is less than 30 . You can also calculate the mean and check. Here is the statcrunch output:

| Variable | N | N* | Mean | Minimum | Q1 | Median | Q3 | Maximum |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| var1 | 15 | 0 | 26.93 | 3.00 | 12.00 | 30.00 | 35.00 | 43.00 |

- no gaps on the stemplot and $1.5 \times I Q R$ rule shows no outliers.

28. Pulse rates of ten students are given below:
$32,60,62,64,66,68,72,76,80,82$
What would be a five-number summary for these pulse rates?
A) $32,64,67,78,82$
B) $32,62,67,76,82$
C) $60,62,70,78,80$
D) $32,62,68,76,82$
E) $32,61,67,78,82$
29. The pulse rate of 32 in the data set in question 28 above, is an outlier. That student has entered his pulse rate incorrectly. His correct pulse rate was 64 . If we correct this outlier, what will happen to the following statistics?
A) Mean remains the same, median remains the same, IQR decreases.
B) Mean increases, median remains the same, IQR increases.
C) Mean increases, median increases and IQR remain the same.
D) Mean increases, median remains the same, IQR decreases
E) Mean increases, median remains the same, IQR remains the same.
30. New recruits to the Canadian military have head circumferences that are Normally distributed with mean of 65 cm , and standard deviation of 4 cm . One percent of the helmets manufactured for the recruits should have circumferences bigger than what size?
A) 63.06 cm
B) 80.9 cm
C) 74.3 cm
D) 91.23 cm
E) 68.9 cm

Solution: $65+4 \times 2.33=74.32$

| Table Z | Second decimal place in $z$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Areas under the | 0.09 | 0.08 | 0.07 | 0.06 | 0.05 | 0.04 | 0.03 | 0.02 | 0.01 | 0.00 | $z$ |
| standard Normal curve |  |  |  |  |  |  |  |  |  | $0.0000^{+}$ | -3.9 |
|  | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | -3.8 |
| - | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | -3.7 |
|  | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0001 | 0.0002 | 0.0002 | -3.6 |
|  | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | -3.5 |
| $z \quad 0$ |  |  |  |  |  |  |  |  |  |  |  |
|  | 0.0002 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | -3.4 |
|  | 0.0003 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0005 | 0.0005 | 0.0005 | -3.3 |
|  | 0.0005 | 0.0005 | 0.0005 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0007 | 0.0007 | -3.2 |
|  | 0.0007 | 0.0007 | 0.0008 | 0.0008 | 0.0008 | 0.0008 | 0.0009 | 0.0009 | 0.0009 | 0.0010 | -3.1 |
|  | 0.0010 | 0.0010 | 0.0011 | 0.0011 | 0.0011 | 0.0012 | 0.0012 | 0.0013 | 0.0013 | 0.0013 | -3.0 |
|  | 0.0014 | 0.0014 | 0.0015 | 0.0015 | 0.0016 | 0.0016 | 0.0017 | 0.0018 | 0.0018 | 0.0019 | -2.9 |
|  | 0.0019 | 0.0020 | 0.0021 | 0.0021 | 0.0022 | 0.0023 | 0.0023 | 0.0024 | 0.0025 | 0.0026 | -2.8 |
|  | 0.0026 | 0.0027 | 0.0028 | 0.0029 | 0.0030 | 0.0031 | 0.0032 | 0.0033 | 0.0034 | 0.0035 | $-2.7$ |
|  | 0.0036 | 0.0037 | 0.0038 | 0.0039 | 0.0040 | 0.0041 | 0.0043 | 0.0044 | 0.0045 | 0.0047 | -2.6 |
|  | 0.0048 | 0.0049 | 0.0051 | 0.0052 | 0.0054 | 0.0055 | 0.0057 | 0.0059 | 0.0060 | 0.0062 | -2.5 |
|  | 0.0064 | 0.0066 | 0.0068 | 0.0069 | 0.0071 | 0.0073 | 0.0075 | 0.0078 | 0.0080 | 0.0082 | -2.4 |
|  | 0.0084 | 0.0087 | 0.0089 | 0.0091 | 0.0094 | 0.0096 | 0.0099 | 0.0102 | 0.0104 | 0.0107 | -2.3 |
|  | 0.0110 | 0.0113 | 0.0116 | 0.0119 | 0.0122 | 0.0125 | 0.0129 | 0.0132 | 0.0136 | 0.0139 | -2.2 |
|  | 0.0143 | 0.0146 | 0.0150 | 0.0154 | 0.0158 | 0.0162 | 0.0166 | 0.0170 | 0.0174 | 0.0179 | -2.1 |
|  | 0.0183 | 0.0188 | 0.0192 | 0.0197 | 0.0202 | 0.0207 | 0.0212 | 0.0217 | 0.0222 | 0.0228 | $-2.0$ |
|  | 0.0233 | 0.0239 | 0.0244 | 0.0250 | 0.0256 | 0.0262 | 0.0268 | 0.0274 | 0.0281 | 0.0287 | -1.9 |
|  | 0.0294 | 0.0301 | 0.0307 | 0.0314 | 0.0322 | 0.0329 | 0.0336 | 0.0344 | 0.0351 | 0.0359 | -1.8 |
|  | 0.0367 | 0.0375 | 0.0384 | 0.0392 | 0.0401 | 0.0409 | 0.0418 | 0.0427 | 0.0436 | 0.0446 | -1.7 |
|  | $0.0455$ | 0.0465 | 0.0475 | 0.0485 | 0.0495 | 0.0505 | 0.0516 | 0.0526 | 0.0537 | 0.0548 | -1.6 |
|  | 0.0559 | 0.0571 | 0.0582 | 0.0594 | 0.0606 | 0.0618 | 0.0630 | 0.0643 | 0.0655 | 0.0668 | $-1.5$ |
|  | 0.0681 | 0.0694 | 0.0708 | 0.0721 | 0.0735 | 0.0749 | 0.0764 | 0.0778 | 0.0793 | 0.0808 | -1.4 |
|  | 0.0823 | 0.0838 | 0.0853 | 0.0869 | 0.0885 | 0.0901 | 0.0918 | 0.0934 | 0.0951 | 0.0968 | -1.3 |
|  | 0.0985 | 0.1003 | 0.1020 | 0.1038 | 0.1056 | 0.1075 | 0.1093 | 0.1112 | 0.1131 | 0.1151 | -1.2 |
|  | 0.1170 | 0.1190 | 0.1210 | 0.1230 | 0.1251 | 0.1271 | 0.1292 | 0.1314 | 0.1335 | 0.1357 | -1.1 |
|  | 0.1379 | 0.1401 | 0.1423 | 0.1446 | 0.1469 | 0.1492 | 0.1515 | 0.1539 | 0.1562 | 0.1587 | $-1.0$ |
|  | 0.1611 | 0.1635 | 0.1660 | 0.1685 | 0.1711 | 0.1736 | 0.1762 | 0.1788 | 0.1814 | 0.1841 | -0.9 |
|  | 0.1867 | 0.1894 | 0.1922 | 0.1949 | 0.1977 | 0.2005 | 0.2033 | 0.2061 | 0.2090 | 0.2119 | -0.8 |
|  | 0.2148 | 0.2177 | 0.2206 | 0.2236 | 0.2266 | 0.2296 | 0.2327 | 0.2358 | 0.2389 | 0.2420 | -0.7 |
|  | 0.2451 | 0.2483 | 0.2514 | 0.2546 | 0.2578 | 0.2611 | 0.2643 | 0.2676 | 0.2709 | 0.2743 | -0.6 |
|  | 0.2776 | 0.2810 | 0.2843 | 0.2877 | 0.2912 | 0.2946 | 0.2981 | 0.3015 | 0.3050 | 0.3085 | -0.5 |
|  | 0.3121 | 0.3156 | 0.3192 | 0.3228 | 0.3264 | 0.3300 | 0.3336 | 0.3372 | 0.3409 | 0.3446 | -0.4 |
|  | 0.3483 | 0.3520 | 0.3557 | 0.3594 | 0.3632 | 0.3669 | 0.3707 | 0.3745 | 0.3783 | 0.3821 | -0.3 |
|  | 0.3859 | 0.3897 | 0.3936 | 0.3974 | 0.4013 | 0.4052 | 0.4090 | 0.4129 | 0.4168 | 0.4207 | -0.2 |
|  | 0.4247 | 0.4286 | 0.4325 | 0.4364 | 0.4404 | 0.4443 | 0.4483 | 0.4522 | 0.4562 | 0.4602 | -0.1 |
|  | 0.4641 | 0.4681 | 0.4721 | 0.4761 | 0.4801 | 0.4840 | 0.4880 | 0.4920 | 0.4960 | 0.5000 | -0.0 |

${ }^{\dagger}$ For $z \leq-3.90$, the areas are 0.0000 to four decimal places.

| Table Z (cont.) |  | Second decimal place in $z$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Areas under the | $z$ | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| standard Normal curve | 0.0 | 0.5000 | 0.5040 | 0.5080 | 0.5120 | 0.5160 | 0.5199 | 0.5239 | 0.5279 | 0.5319 | 0.5359 |
|  | 0.1 | 0.5398 | 0.5438 | 0.5478 | 0.5517 | 0.5557 | 0.5596 | 0.5636 | 0.5675 | 0.5714 | 0.5753 |
| - | 0.2 | 0.5793 | 0.5832 | 0.5871 | 0.5910 | 0.5948 | 0.5987 | 0.6026 | 0.6064 | 0.6103 | 0.6141 |
| , | 0.3 | 0.6179 | 0.6217 | 0.6255 | 0.6293 | 0.6331 | 0.6368 | 0.6406 | 0.6443 | 0.6480 | 0.6517 |
| ) | 0.4 | 0.6554 | 0.6591 | 0.6628 | 0.6664 | 0.6700 | 0.6736 | 0.6772 | 0.6808 | 0.6844 | 0.6879 |
| 0 z |  |  |  |  |  |  |  |  |  |  |  |
|  | 0.5 | 0.6915 | 0.6950 | 0.6985 | 0.7019 | 0.7054 | 0.7088 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |
|  | 0.6 | 0.7257 | 0.7291 | 0.7324 | 0.7357 | 0.7389 | 0.7422 | 0.7454 | 0.7486 | 0.7517 | 0.7549 |
|  | 0.7 | 0.7580 | 0.7611 | 0.7642 | 0.7673 | 0.7704 | 0.7734 | 0.7764 | 0.7794 | 0.7823 | 0.7852 |
|  | 0.8 | 0.7881 | 0.7910 | 0.7939 | 0.7967 | 0.7995 | 0.8023 | 0.8051 | 0.8078 | 0.8106 | 0.8133 |
|  | 0.9 | 0.8159 | 0.8186 | 0.8212 | 0.8238 | 0.8264 | 0.8289 | 0.8315 | 0.8340 | 0.8365 | 0.8389 |
|  | 1.0 | 0.8413 | 0.8438 | 0.8461 | 0.8485 | 0.8508 | 0.8531 | 0.8554 | 0.8577 | 0.8599 | 0.8621 |
|  | 1.1 | 0.8643 | 0.8665 | 0.8686 | 0.8708 | 0.8729 | 0.8749 | 0.8770 | 0.8790 | 0.8810 | 0.8830 |
|  | 1.2 | 0.8849 | 0.8869 | 0.8888 | 0.8907 | 0.8925 | 0.8944 | 0.8962 | 0.8980 | 0.8997 | 0.9015 |
|  | 1.3 | 0.9032 | 0.9049 | 0.9066 | 0.9082 | 0.9099 | 0.9115 | 0.9131 | 0.9147 | 0.9162 | 0.9177 |
|  | 1.4 | 0.9192 | $0.9207$ | 0.9222 | 0.9236 | 0.9251 | 0.9265 | 0.9279 | 0.9292 | 0.9306 | 0.9319 |
|  | 1.5 | 0.9332 | 0.9345 | 0.9357 | 0.9370 | 0.9382 | 0.9394 | 0.9406 | 0.9418 | 0.9429 | 0.9441 |
|  | $1.6$ | $0.9452$ | $0.9463$ | $0.9474$ | $0.9484$ | 0.9495 | $0.9505$ | 0.9515 | 0.9525 | 0.9535 | $0.9545$ |
|  | 1.7 | 0.9554 | 0.9564 | 0.9573 | 0.9582 | 0.9591 | 0.9599 | 0.9608 | $0.9616$ | 0.9625 | 0.9633 |
|  | 1.8 | 0.9641 | 0.9649 | 0.9656 | 0.9664 | 0.9671 | 0.9678 | 0.9686 | 0.9693 | 0.9699 | 0.9706 |
|  | 1.9 | 0.9713 | $0.9719$ | 0.9726 | 0.9732 | 0.9738 | 0.9744 | 0.9750 | 0.9756 | 0.9761 | 0.9767 |
|  | 2.0 | 0.9772 | 0.9778 | 0.9783 | 0.9788 | 0.9793 | 0.9798 | 0.9803 | 0.9808 | 0.9812 | 0.9817 |
|  | $2.1$ | $0.9821$ | $0.9826$ | $0.9830$ | $0.9834$ | $0.9838$ | $0.9842$ | $0.9846$ | 0.9850 | 0.9854 | 0.9857 |
|  | 2.2 | 0.9861 | 0.9864 | 0.9868 | 0.9871 | 0.9875 | 0.9878 | 0.9881 | 0.9884 | 0.9887 | 0.9890 |
|  | 2.3 | 0.9893 | 0.9896 | 0.9898 | 0.9901 | 0.9904 | 0.9906 | 0.9909 | 0.9911 | 0.9913 | 0.9916 |
|  | 2.4 | 0.9918 | 0.9920 | 0.9922 | 0.9925 | 0.9927 | 0.9929 | 0.9931 | 0.9932 | 0.9934 | 0.9936 |
|  | 2.5 | 0.9938 | 0.9940 | 0.9941 | 0.9943 | 0.9945 | 0.9946 | 0.9948 | 0.9949 | 0.9951 | 0.9952 |
|  | $2.6$ | $0.9953$ | $0.9955$ | $0.9956$ | $0.9957$ | $0.9959$ | 0.9960 | $0.9961$ | $0.9962$ | 0.9963 | 0.9964 |
|  | $2.7$ | $0.9965$ | $0.9966$ | $0.9967$ | $0.9968$ | $0.9969$ | 0.9970 | $0.9971$ | $0.9972$ | $0.9973$ | $0.9974$ |
|  | $2.8$ | $0.9974$ | $0.9975$ | $0.9976$ | $0.9977$ | $0.9977$ | $0.9978$ | $0.9979$ | $0.9979$ | $0.9980$ | $0.9981$ |
|  | 2.9 | 0.9981 | 0.9982 | 0.9982 | 0.9983 | 0.9984 | 0.9984 | 0.9985 | 0.9985 | 0.9986 | 0.9986 |
|  | 3.0 | 0.9987 | 0.9987 | 0.9987 | 0.9988 | 0.9988 | 0.9989 | 0.9989 | 0.9989 | 0.9990 | 0.9990 |
|  | 3.1 | 0.9990 | 0.9991 | 0.9991 | 0.9991 | 0.9992 | 0.9992 | 0.9992 | 0.9992 | 0.9993 | 0.9993 |
|  | 3.2 | 0.9993 | 0.9993 | 0.9994 | 0.9994 | 0.9994 | 0.9994 | 0.9994 | 0.9995 | 0.9995 | 0.9995 |
|  | $3.3$ | $0.9995$ | $0.9995$ | $0.9995$ | $0.9996$ | $0.9996$ | $0.9996$ | $0.9996$ | $0.9996$ | 0.9996 | 0.9997 |
|  | 3.4 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9998 |
|  | 3.5 | 0.9998 | 0.9998 | 0.9998 | 0.9998 | 0.9998 | 0.9998 | 0.9998 | 0.9998 | 0.9998 | 0.9998 |
|  | 3.6 | 0.9998 | 0.9998 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 |
|  | 3.7 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 |
|  | 3.8 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 | 0.9999 |
|  | 3.9 | $1.0000^{+}$ |  |  |  |  |  |  |  |  |  |
|  | ${ }^{+}$For | $\geq 3.90$, | the area | are 1.00 | 00 to fou | ur decim | al places |  |  |  |  |

