

Example: Find the mean value of the random variable  $X$ :

$X$	1	4	5
$p$	0.3	0.5	0.2

$$\mu_x = 1 \cdot 0.3 + 4 \cdot 0.5 + 5 \cdot 0.2$$

$$= 0.3 + 2 + 1 = 3.3$$

$$\begin{aligned} \sigma_x^2 &= (1 - 3.3)^2 \cdot 0.3 + (4 - 3.3)^2 \cdot 0.5 \\ &\quad + (5 - 3.3)^2 \cdot 0.2 = 2.41 \end{aligned}$$

$$\sigma_x = \sqrt{2.41} = 1.55$$

Example: Given two independent random variables, X and Y:

	Mean	SD
X	10	2
Y	20	5

$$\mu_{a+bX} = a + b\mu_X$$

$$\sigma_{a+bX} = b\sigma_X$$

Find the mean and SD of

(a)  $3X$

$$\mu_{3X} = 3\mu_X = 3 \cdot 10 = 30$$

$$\sigma_{3X} = 3\sigma_X = 3 \cdot 2 = 6$$

(b)  $Y+6$

$$\mu_{Y+6} = \mu_Y + 6 = 20 + 6 = 26$$

$$\sigma_{Y+6} = \sigma_Y = 5$$

(c)  $X-Y$

$$\mu_{X-Y} = \mu_X - \mu_Y = 10 - 20 = -10$$

$$\sigma_{X-Y} = \sqrt{\sigma_{X-Y}^2} = \sqrt{\sigma_X^2 + \sigma_Y^2} = \sqrt{2^2 + 5^2} = \sqrt{29}$$