## **Indicator functions**: This notation is not in the text!

Let A be a set of real numbers. Then the **indicator function** for A is defined by

$$I_A(x) = I\{x \in A\} = \begin{cases} 1 & \text{for } x \in A \\ 0 & \text{for } x \notin A \end{cases}$$

Two important properties of indicator functions are  $I_A(x)$   $I_B(x) = I_{A \cap B}(x)$  and if g(x) is a real valued function,

$$g(x) \ I_A(x) = \begin{cases} g(x) \ \text{for } x \in A \\ 0 \ \text{for } x \notin A \end{cases}$$

**Def**. The **support** of a random variable is the set of x values for which f(x) > 0.

In this class, probability distributions and probability density functions will always be defined for all real x, and will include indicators for their support.

For example, where the book might write

$$f(x) = \begin{cases} \frac{x}{6} & \text{for } x = 1, 2, 3 \\ 0 & \text{otherwise} \end{cases}$$

we will write

$$f(x) = \frac{x}{6} I\{x = 1,2,3\}.$$

And the gamma density may be written

$$f(x) = \frac{1}{\beta^{\alpha} \, \Gamma(\alpha)} \; e^{-x/\beta} \, x^{\alpha\text{-}1} \; \; I(x{>}0). \label{eq:force}$$