The next weeks

March 16	§10.7 Semiparametric models
March 23	Generalized additive models and lasso
March 30	Finishing pieces, + review

Homework 3: due April 2, 5 pm

(updated March 20) Final Test: April 17, 1 - 3 pm

When answering questions requiring numerical work, the results are to be reported in a narrative summary, in your own works. Tables and Figures may be included, but must be formatted along with the text. **Do not include in this summary printouts of computer code**. Analysis of variance/deviance tables, tables of coefficients and their estimated standard errors, and other output should be formatted separately and reported only to the relevant number of significant digits. All computer code used to obtain the results summarized in the response should be provided as an appendix.

- (Faraway Extending the Linear Model with R, Ch. 11): The dataset teengamb in the package faraway gives data on annual gambling expenditure per year (in pounds) (gamble), with several covariates: sex (0 = M, 1 = F), status (a score reflecting socioeconomic status), income (pounds per week), verbal (a score from 0 -12 on a test of verbal ability). Of interest is which covariates are associated with gambling expenditure.
 - (a) Using an appropriate parametric model, investigate the relationship between gambling and other factors, and summarize your conclusions in non-technical language, accompanied by no more than 3 tables and 3 figures.
 - (b) Investigate the use of non-parametric smoothing techniques on the data; do any insights emerge from this approach that were missed in the analysis in part (a)? Summarize your results for this part of the question by describing which methods you used, what information they provided, and whether or not they altered the conclusions from part (a). Your text should not be more than two pages, and you may include up to four figures.
- (a) Show that if y_{ij} are independently distributed as as Poisson distribution with means μ_{ij}, i = 1,..., I; j = 1..., J, that y_{ij} given y_{i+} are distributed as multinomial, with sample size y_{i+} and probability vector π_{ij} = μ_{ij}/μ_{i+}.
 - (b) If log µ_{ij} = μ + α_i + β_j, where α₁ = 0 and β_i = 0, show that the residual deviance from this model is the same as the log-likelihood ratio statistic for testing independence in a multinomial model. Your task is to verify it algebraically; it has been verified numerically for HW2Q4 by Wei Lin, who showed that the observed and (fitted) values for the 2 × 2 table of breathlessness and wheze, ignoring age, are as follows, whether computed using the multinomial model or the Poisson glm.

	Wheeze			
Breathlessness	N	Y		
N	14022 (12680.9)	1833 (3174.1)		
V	600 (1041 1)	1007 (405.0)		

Kernel smoothing

- regression smoothing $y_j = g(x_j) + \epsilon_j$
- $\hat{g}(x_0) = \sum_{j=1}^n S(x_0; x_j, h) y_j$ $S(x_0; x_j, h)$ from $(X^T W X)^{-1} X^T W$
- local likelihood: $y_j \sim f(\cdot; \beta, x_j)$

$$\max_{\beta} \sum \log f(y_j; \beta, x_j) \longrightarrow \max_{\beta} \sum \frac{1}{h} w\left(\frac{x_j - x_0}{h}\right) \log f(y_j; \beta, x_j)$$

b

Example 10.32



Figure 10.17 Local fit to the toxoplasmosis dat The left panel shows fitt probabilities $\widehat{\pi}(x)$, with the fit of local linear logistic model with h = 400 (solid) and 0.95 pointwise confidence bands (dots). Also show is the local linear fit with h = 300 (dashes). The right panel shows the loc quadratic fit with h = 40and its 0.95 confidence band. Note the increased variability due to the quadratic fit, and its stronger curvature at the boundaries.

Flexible modelling using basis expansions

(§10.7.2)

•
$$y_j = g(x_j) + \epsilon_j$$

Flexible linear modelling

$$g(x) = \sum_{m=1}^{M} \beta_m h_m(x)$$

- ► This is called a linear basis expansion, and *h_m* is the *m*th basis function
- For example if X is one-dimensional: $g(x) = \beta_0 + \beta_1 x + \beta_2 x^2$, or $g(x) = \beta_0 + \beta_1 \sin(x) + \beta_2 \cos(x)$, etc.
- Simple linear regression has $h_1(x) = 1$, $h_2(x) = x$

Piecewise polynomials

▶ piecewise constant basis functions $h_1(x) = I(x < \xi_1), \quad h_2(x) = I(\xi_1 \le x < \xi_2),$ $h_3(x) = I(\xi_2 \le x)$

equivalent to fitting by local averaging

- piecewise linear basis functions , with constraints $h_1(x) = 1$, $h_2(x) = x$ $h_3(x) = (x - \xi_1)_+$, $h_4(x) = (x - \xi_2)_+$
- windows defined by knots ξ_1, ξ_2, \ldots
- ► piecewise cubic basis functions $h_1(x) = 1, h_2(x) = x, h_3(x) = x^2, h_4(x) = x^3$
- continuity $h_5(x) = (x \xi_1)^3_+, \quad h_6(x) = (x \xi_2)^3_+$
- continuous function, continuous first and second derivatives



FIGURE 5.1. The top left panel shows a piecewise constant function fit to some artificial data. The broken vertical lines indicate the positions of the two knots ξ_1 and ξ_2 . The blue curve represents the true function, from which the data were

Piecewise Cubic Polynomials



FIGURE 5.2. A series of piecewise-cubic polynomials, with increasing orders of continuity.

Example: earthquake data

```
> data(guake,package="SMPracticals")
> guake
             time mag
        40.08333 6.0
2
       162.38889 6.9
3
       210.22917 6.0
       303.85417 6.2
4
> with(quake, plot(log(1/time),mag))
    8.5
                         0
            0
              0
    8.0
          0
                     0
                        0
               0
    7.5
              ത
                  0
              0
                      0 0
                 0
mag
              0
                00
          \infty
                      റത
                                   0
             രത്ത്ര ര
    0.7
                      ത
                         0
                              0
                                                  0
              ത
                 000 0
           നറന്നത
                       00
                           0
         000000
               നാതാ
                              0
           തത്തുള്ളറ
                      0
    3.5
                        0 0
                                 0
         റ റണ്ണാറതറ
                  നാറ
                       0
                                     0
                              0
                                         00 0
         അന്തലം
                തെ റററത
                         ഹറ
                              0
                                     0
                                             0
              a
    6.0
                                                0
            0
                                                             0
            -10
                    -9
                            -8
                                   -7
                                           -6
                                                  -5
                                                          -4
```

STA 2201S: Mar 23, 2012

Cubic splines

- truncated power basis of degree 3
- need to choose number of knots K and placement of knots ξ_1, \dots, ξ_K
- construct features matrix using truncated power basis set
- use constructed matrix as set of predictors

```
> with(guake, bs(log(1/time))[1:10,])
     #bs(x) with no other arguments just gives a single cubic polynomial
      [1,] 0.0000000 0.0000000 1.0000000
      [2,] 0.1018013 0.3903714 0.4989780
      [3,] 0.1359705 0.4189773 0.4303434
      [4,] 0.1884790 0.4408886 0.3437743
      [5,] 0.2056632 0.4436068 0.3189471
      [6,] 0.2108533 0.4440520 0.3117209
      [7,] 0.2522139 0.4418128 0.2579802
      [8,] 0.2752334 0.4363260 0.2305684
      [9,] 0.3398063 0.4045238 0.1605223
     [10,] 0.3398083 0.4045224 0.1605203
     attr(, "degree")
     [1] 3
     attr(, "knots")
     numeric(0)
     attr(, "Boundary.knots")
     [1] -10.454784 -3.690961
     attr(, "intercept")
     [1] FALSE
STA 22015: Mar 23(2012 ass")
                   "booic" "mot viv"
```

... cubic splines

```
> with(quake,bs(log(1/time), df=5)[1:10,])
   # gives a proper cubic spline basis, here with 5 df
         1
                     2
                               3
                                          4
                                                    5
    [1,] 0 0.0000000 0.000000 0.0000000 1.0000000
    [2,] 0 0.01110655 0.1250814 0.4247847 0.4390274
    [3,] 0 0.01846075 0.1661869 0.4486889 0.3666635
    [4,] 0 0.03370916 0.2283997 0.4600092 0.2778819
    [5,] 0 0.03989014 0.2484715 0.4585984 0.2530400
    [6,] 0 0.04188686 0.2545024 0.4577416 0.2458691
    [7,1 0 0.06023519 0.3019733 0.4443033 0.1934881
    [8,] 0 0.07263434 0.3278645 0.4319962 0.1675050
    [9,] 0 0.11941791 0.3975881 0.3789378 0.1040562
   [10,] 0 0.11941975 0.3975902 0.3789357 0.1040544
   . . .
   attr(, "degree")
   [1] 3
   attr(, "knots")
   33.33338 66.666678
   -9.943294 -9.520987
   attr(, "Boundary.knots")
STA 22015: Harl23, 2012 0.454784 -3.690961
```

... earthquake data

```
> guake.bs = lm(mag ~ bs(log(1/time),df=5),data = guake)
> guake.pred = predict(guake.bs, se.fit = TRUE, interval = "confidence")
> quake.pred
Śfit
         fit
                 lwr
                           upr
  5.962665 5.216283 6.709047
2
  6.279641 5.979190 6.580092
З
   6.323859 6.042772 6.604946
> lines(log(1/quake$time),quake.pred[[1]][,1])
> lines(log(1/guake$time), guake.pred[[1]][,2], lty=2)
> lines(log(1/quake$time),quake.pred[[1]][,3], lty=2)
> quake.lo = loess(mag ~ log(1/time), data = quake)
> quake.lopred = predict(quake.lo, se=T)
```



12/1

B-splines and N-splines

- The B-spline basis equivalent to the truncated power basis
- In R library(splines): bs(x, df=NULL, knots=NULL, degree=3, intercept=FALSE, Boundary.knots=range(x))
- Must specify either df or knots. For the B-spline basis, # knots = df - degree and degree is usually 3
- Natural cubic splines are linear at the end of the range
- ns(x, df=NULL, knots=NULL, degree=3, intercept=FALSE, Boundary.knots=range(x))
- For natural cubic splines, # knots = df 1

... regression splines

The individual coefficients don't mean anything, we need to evaluate groups of coefficients. For example





... regression splines

- easily extended to multiple regression, and generalized linear models
- example: data(heart, package =
 "ElemStatLearn")

```
> heart[1:5,]
   row.names sbp tobacco ldl adiposity famhist typea obesity
                                                                                    49 25.30
1
                1 160 12.00 5.73 23.11 Present
2
               2 144 0.01 4.41 28.61 Absent 55 28.87

        3
        118
        0.08
        3.48
        32.28
        Present
        52
        29.14

        4
        170
        7.50
        6.41
        38.03
        Present
        51
        31.99

        5
        134
        13.60
        3.50
        27.78
        Present
        60
        25.99

3
4
5
   alcohol age chd
   97.20 52 1
1
2
   2.06 63 1
3 3.81 46 0
  24.26 58 1
4
5
    57.34 49 1
```

... heart data

```
> heart.ns = qlm (chd ~ ns(sbp,4) + ns(tobacco,4) + ns(ldl,4) + famhist + ns(obesity, 4) +
    + ns(age,4), family=binomial)
    > summarv(heart.ns)
    Call:
    glm(formula = chd ~ ns(sbp, 4) + ns(tobacco, 4) + ns(ldl, 4) +
        famhist + ns(obesity, 4) + ns(age, 4), family = binomial)
    Deviance Residuals.
        Min
                 10 Median 30
                                       Max
    -1.7216 -0.8322 -0.3777 0.8870 2.9694
    Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
                  -2.265534 2.367227 -0.957 0.338547
    (Intercept)
    ns(sbp, 4)1 -1.474172 0.843870 -1.747 0.080652.
    ns(sbp, 4)2 -1.351182 0.759548 -1.779 0.075251.
    ns(sbp, 4)3 -3.729348
                              2.021064 -1.845 0.065003 .
    ns(sbp, 4)4 1.381701
                              0.995268 1.388 0.165055
    ns(tobacco, 4)1 0.654109
                              0.453248 1.443 0.148975
    ns(tobacco, 4)2 0.392582
                              0.892628 0.440 0.660079
    ns(tobacco, 4)3 3.335170
                              1.179656 2.827 0.004695 **
    ns(tobacco, 4)4 3.845611
                              2.386584 1.611 0.107104
    ns(ldl, 4)1
                   1.921215
                              1.311052
                                        1.465 0.142812
    ns(ldl, 4)2
                   1.783272
                              1.014883
                                        1.757 0.078897 .
    ns(ldl, 4)3 4.623680
ns(ldl, 4)4 3.354692
                               2.972938
                                        1.555 0.119885
                              1.447217 2.318 0.020448 *
    famhistPresent 1.078507
                              0.237685
                                        4.538 5.69e-06 ***
    ns(obesity, 4)1 -3.089393
                              1.707207
                                        -1.810 0.070355 .
    ns(obesity, 4)2 -2.385045
                              1.200450
                                        -1.987 0.046945 *
    ns(obesity, 4)3 -4.998882
                               3.796264
                                        -1.317 0.187909
    no/ohooity 4)4 0 000100
                               1 751107 0 005 0 005050
STA 22018 906728 920124) 1
                    2.628298
                               1.116674
                                         2.354 0.018588 *
                                                                                        17/1
```

```
> update(heart.ns, . ~ . - ns(sbp,4))
Call: glm(formula = chd ~ ns(tobacco, 4) + ns(ldl, 4) + famhist + ns(obesity, 4) + ns(a
Coefficients:
   (Intercept) ns(tobacco, 4)1 ns(tobacco, 4)2 ns(tobacco, 4)3
      -3.91758
                      0.61696
                                     0.46188
                                                     3.51363
ns(tobacco, 4)4 ns(ldl, 4)1 ns(ldl, 4)2 ns(ldl, 4)3
       3.82464
                      1.70945
                                     1.70659
                                                     4.19515
   ns(ldl, 4)4 famhistPresent ns(obesity, 4)1 ns(obesity, 4)2
       2.90793
                      0.99053
                                     -2.93143
                                                    -2.32793
ns(obesity, 4)3 ns(obesity, 4)4 ns(age, 4)1 ns(age, 4)2
      -4.87074
                    -0.01103
                                    2.52772 3.12963
   ns(age, 4)3 ns(age, 4)4
       7 34899
                      1 53433
Degrees of Freedom: 461 Total (i.e. Null); 444 Residual
Null Deviance.
                 596 1
Residual Deviance: 467.2 ATC: 503.2
> 467.2 - 458.1
[1] 9.1
> pchisq(9.1,df=4)
[1] 0.941352
> 1-.Last.value
[1] 0.05864798 # compare Table 5.1
```

The function step does all this for you:

```
> step(heart.ns)
Start: ATC=502.09
chd \sim ns(sbp, 4) + ns(tobacco, 4) + ns(ldl, 4) + famhist + ns(obesity,
   4) + ns(age, 4)
               Df Deviance ATC
                   458.09 502.09
<none>
- ns(obesity, 4) 4 466.24 502.24
- ns(sbp, 4) 4 467.16 503.16
- ns(tobacco, 4) 4 470.48 506.48
- ns(ldl, 4) 4 472.39 508.39
- ns(age, 4) 4 481.86 517.86
- famhist 1 479.44 521.44
> anova(heart.ns)
Analysis of Deviance Table
Model: binomial, link: logit
Response: chd
Terms added sequentially (first to last)
              Df Deviance Resid. Df Resid. Dev
                              461
                                   596.11
NULL
              4 19.26
ns(sbp, 4)
                             457 576.85
               4 46.90
ns(tobacco, 4)
                            453 529.95
                           449 510.87
448 485.58
ns(ldl, 4) 4 19.08
famhist 1 25.29
                             444 481.86
ns(obesity, 4) 4 3.73
ns(age, 4) 4 23.77
                             440
                                    458.09
```

Smoothing splines §10.7.2

•
$$y_j = g(t_j) + \epsilon_j, \quad j = 1, \ldots, n$$

• choose $g(\cdot)$ to solve

$$\min_{g} \sum_{j=1}^{n} \frac{\{y - g(t_j)\}^2}{2\sigma^2} - \frac{\lambda}{2\sigma^2} \int_{a}^{b} \{g''(t)\}^2 dt, \quad \lambda > 0$$

- solution is a cubic spline, with knots at each observed x_i value
- see Figure 10.18 for a non-regularized solution
- has an explicit, finite dimensional solution
- $\hat{g} = \{\hat{g}(t_1), \dots, \hat{g}(t_n)\} = (I + \lambda K)^{-1} y$
- *K* is a symmetric $n \times n$ matrix of rank n 2



log(1/time)

... smoothing splines

```
> guake$int = log(1/guake$time)
> guake[1:4,]
      time mag int
1 40.08333 6.0 -3.690961
2 162.38889 6.9 -5.089994
3 210.22917 6.0 -5.348198
4 303.85417 6.2 -5.716548
> attach(guake)
> plot(int, mag)
> guake.ss2 = smooth.spline(x = int, y = mag, df = 5)
> lines(guake.ss2, col="red")
> guake.ss3
Call:
smooth.spline(x = int, y = mag, cv = TRUE)
Smoothing Parameter spar= 1.499945 lambda= 0.0001340604 (25 iterations)
Equivalent Degrees of Freedom (Df): 11.35023
Penalized Criterion: 64 57512
PRESS: 0.1730025
> lines(guake.ss3, col="blue")
```

... smoothing splines

An example from the R help file for smooth.spline:

```
> data(cars)
> attach(cars)
> plot(speed, dist, main = "data(cars) & smoothing splines")
> cars.spl <- smooth.spline(speed, dist)</pre>
> (cars.spl)
Call·
smooth.spline(x = speed, v = dist)
Smoothing Parameter spar= 0.7801305 lambda= 0.1112206 (11 iterations)
Equivalent Degrees of Freedom (Df): 2.635278
Penalized Criterion: 4337.638
GCV: 244.1044
> lines(cars.spl, col = "blue")
       lines(smooth.spline(speed, dist, df=10), lty=2, col = "red")
>
      legend(5,120,c(paste("default [C.V.] => df =",round(cars.spl$df,1)),
>
                      "s( * , df = 10)"), col = c("blue", "red"), ltv = 1:2,
+
              bg='bisgue')
+
> detach()
```









Multidimensional splines

- so far we are considering just 1 X at a time
- for regression splines we replace each X by the new columns of the basis matrix
- for smoothing splines we get a univariate regression
- it is possible to construct smoothing splines for two or more inputs simultaneously, but computational difficulty increases rapidly
- these are called thin plate splines
- alternative:

 $E(Y | X_1, ..., X_p) = f_1(X_1) + f_2(X_2) + \cdots + f_p(X_p)$ additive models

▶ binary response: logit{ $E(Y | X_1, ..., X_p)$ } = $f_1(X_1) + f_2(X_2) + \cdots + f_p(X_p)$ generalized additive models

Which smoothing method?

- basis functions: natural splines, Fourier, wavelet bases
- regularization via cubic smoothing splines
- kernel smoothers: locally constant/linear/polynomial
- adaptive bandwidth, running medians, running *M*-estimates
- Dantzig selector, elastic net, rodeo (Lafferty & Wasserman, 2008)
- Faraway (2006) Extending the Linear Model:
 - with very little noise, a small amount of local smoothing (e.g. nearest neighbours)
 - with moderate amounts of noise, kernel and spline methods are effective
 - with large amounts of noise, parametric methods are more attractive
- "It is not reasonable to claim that any one smoother is better than the rest"
 - loess is robust to outliers, and provides smooth fits
 - spline smoothers are more efficient, but potentially sensitive

to outliers

Ethics and Statistics



Chance Magazine, 2011 # 4 and 2012 # 1

... ethics

Open Data and Open Methods

· Columns, Ethics and Statistics



An ethics problem arises when you are considering an action that (a) benefits you or some cause you support, (b) hurts or reduces benefits to others, and (c) violates some rule. Other definitions are possible; there is a vast literature on professional ethics that I will not discuss, instead focusing here on my own perspective as a statistician.

"In future columns, I would like to explore many dimensions of ethics, including those that arise in clinical research and statistical analysis, to problems involving probability and uncertainty, as well as more general concerns such as plagiarism and misrepresentation of research findings"

... ethics

Example: An Unethical Refusal to Share Data

"Before attempting any sort of quantitative treatment, however, I will tell some stories. The story for the present column concerns the ethical imperative to share data. ... A bit more than 20 years ago, I attended – as a PhD student – a statistics conference on the health effects of low-frequency electromagnetic fields."

"The treatment appeared to have an effect, and it varied by frequency, not in any obvious way, but perhaps in some manner that made sense given the underlying biophysics. Figure 1a shows the basic findings of Blackman et al., in which they summarized their results based on the statistical significance level of their estimate at each frequency."



"From my statistical training, I was suspicious of using significance levels in this way – indeed, several years later, Hal Stern and I wrote a paper, "The Difference Between 'Significant' and 'Not Significant' Is Not Itself Statistically Significant" – and so I made a new graph showing estimates and confidence intervals, shown here as Figure 1b."

... ethics

"I need to respond to the column by Andrew Gelman about ethics (Vol. 24, No. 4). Most of the column is about a paper published by the principal investigator, Carl Blackman, and me, as the statistician on the project. There are basically two parts to his column. The first is a claim of us being unethical and the second is his assertion of a flawed statistical analysis."

"Gelman says the analysis was flawed and, as he pointed out several times, his "proof" seems to be that he had a PhD (although not at the time) and I only had a master's degree."

"Gelman is correct that ethics is important. We should all be ethical in our research, and so too should we be ethical in our complaints about ethics." ... Dennis House

... ethics

"Dr. Gelman levels the charge, 20 years after the fact, that I violated the principle of openness in scientific research by denying his request to send him copies of my logbooks and that I designed experiments and data analyses that led to a "waste of effort," presumably because I and my coworker misapplied statistical principles in the analysis of the experimental findings. Both assertions are based on misleading and incomplete information, and in my view, are groundless."

"The speculative use of p-values to highlight features of the data was far from "a waste of effort"; rather, it led ... to scientific discovery that has had substantial, beneficial consequences for expanding the understanding of how electromagnetic fields can influence biological systems and processes."

"Perhaps there are even good reasons why the statistically sophisticated neuroscience research community, in some cases, still draws conclusions from the differences between significance levels."... Carl Blackman

60 Minutes

Anil Potti, Duke University

from Wikipedia, "Potti is alleged to have engaged in scientific misconduct while a cancer researcher at both Duke University's Medical Center and School of Medicine. He resigned in November 2010 after Duke suspended him, terminated the clinical trials based on his research and retracted his published data. A scientific misconduct investigation is ongoing."

from Eric, "Kevin Baggerly and Kevin Coombes from the University of Texas MD Anderson Cancer Center were the researchers who made significant contributions in recognizing this fraud by unsuccessfully trying to reconstruct Potti's results with his data."

... 60 Minutes



The Annals of Applied Statistics 2009, Vol. 3, No. 4, 1309–1334 DOI: 10.1214/09-AOAS291 © Institute of Mathematical Statistics, 2009

DERIVING CHEMOSENSITIVITY FROM CELL LINES: FORENSIC BIOINFORMATICS AND REPRODUCIBLE RESEARCH IN HIGH-THROUGHPUT BIOLOGY

BY KEITH A. BAGGERLY¹ AND KEVIN R. COOMBES²

University of Texas

High-throughput biological assays such as microarrays let us ask very detailed questions about how discases operate, and promise to let us personalize therapy. Data processing, however, is often not described well enough to allow for exact reproduction of the results, leading to exercises in "forensic bioinformatics" where aspects of raw data and reported results are used to in-

"In this report we examine several related papers purporting to use microarray-based signatures of drug sensitivity derived from cell lines to predict patient response. Patients in clinical trials are currently being allocated to treatment arms on the basis of these results. However, we show in five case studies that the results incorporate several simple errors that may be putting patients at risk."

NY Times Link

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dosages and treatment are not eligible for patent protection.					in LINKE	DIN					
Writing	, for t	the court, J	ustice S	tephen G. I	Breyer sai	d natural l	aws may	SIGN E-MAI	IN TO		
not be	paten	ted standin	g alone	or in conn	action wit	•	es that	-			
involve					ection wit	h processe	o Linut	台 PRINT			
S. Mar 22, 201	"wel	l-understoo	d. rout	ine, conven	tional act	h processe ivity."			INTS		8/4